

Graph

A graph is a non linear data structure, which consists of points known as nodes (vertices) and set of links known as edges (Arcs) which connects the vertices.

Or

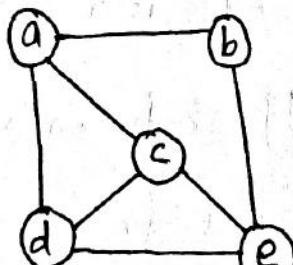
A Graph $G_1 = (V, E)$ is composed of

V : set of vertices

E : set of edges connecting the vertices in V .

An edge $e = (u, v)$ is a pair of vertices.

Example :



$$V = \{a, b, c, d, e\}$$

$$E = \{(a, b), (a, c), (a, d), (b, e), (c, d), (c, e), (d, e)\}$$

$$G_1 = (V, E)$$

Graph Terminology :

Vertex: An individual data element of a graph is called as vertex. vertex is also known as node. In above example graph, a, b, c, d and e are known as vertices.

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Edge :— An edge is a connecting link between two vertices.

Edge is also known as Arc. In above graph, the link between vertices a and b is represented as (a, b) .

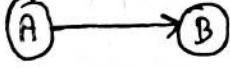
Edges are three types

↳ **undirected Edge** — An undirected edge is a bidirectional edge. If there is an undirected edge between vertices A and B then edge (A, B) is equal to edge (B, A) .

ex:  : $(A, B) = (B, A)$

↳ **Directed Edge** — A directed edge is a unidirectional edge. If there is a directed edge between vertices A and B then edge (A, B) is not equal to edge (B, A)

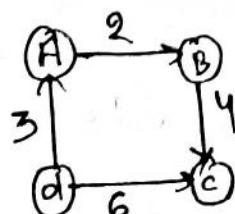
ex:

 : edge (A, B)

 : edge (B, A) So, $\text{edge}(A, B) \neq \text{edge}(B, A)$

↳ **weighted Edge** — A weighted edge is an edge with cost on it.

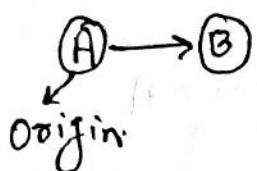
ex:



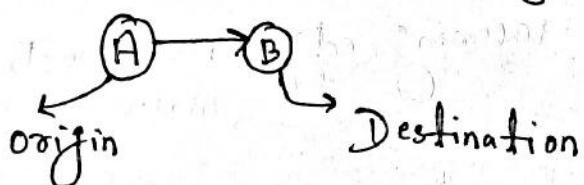
In this example edge (A, B) is associated with cost 2.

- ↳ End vertices or End points : The two vertices joined by edge are called end vertices (or end points) of that edge
- ↳ Origin : if a edge is directed, its first endpoint is said to be the origin of it

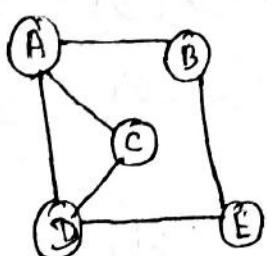
ex:



- ↳ Destination : if a edge is directed, its first endpoint is said to be the origin of it and the other end point is said to be the destination of that edge.



- ↳ Adjacent : if there is an edge between vertices A and B then both A and B are said to be adjacent. In other words, vertices A and B are said to be adjacent if there is an edge between them.



Adjacent vertices of A : B, C and D

" " B : A and E

" " C : A and D

" " D : A, C and E

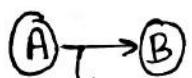
" " E : B and D.

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↳ Incident: Edge is said to be incident on a vertex if the vertex is one of the endpoints of that edge.

↳ Outgoing Edge: A directed edge is said to be outgoing edge on its origin vertex.

ex:



outgoing edge of vertex A

↳ Incoming Edge: A directed edge is said to be incoming edge on its destination vertex.

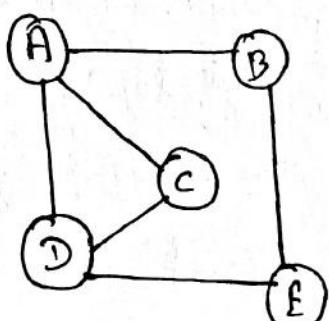
ex:



incoming edge on vertex B.

↳ Degree: Total number of edges connected to a vertex is said to be degree of that vertex.

ex:



$$d(A) = 3 \quad d(C) = 2$$

$$d(B) = 2 \quad d(D) = 3$$

$$d(E) = 2$$

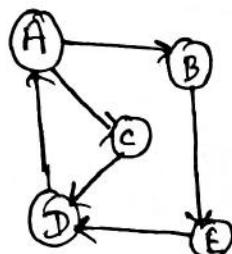
Note: → Sum of the degrees of the vertices is equal to twice the number of edges.

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Indegree: Total number of incoming edges connected to a vertex is said to be indegree of that vertex.

Outdegree: Total number of outgoing edges connected to a vertex is said to be outdegree of that vertex.

Ex:



$$\text{deg}_{\text{in}}(A) = 1 \quad \text{deg}_{\text{out}}(A) = 2$$

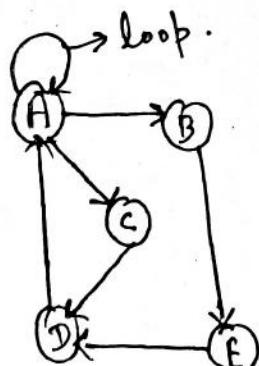
$$\text{deg}_{\text{in}}(B) = 1 \quad \text{deg}_{\text{out}}(B) = 1$$

$$\text{deg}_{\text{in}}(C) = 1, \text{deg}_{\text{out}}(C) = 1$$

$$\text{deg}_{\text{in}}(D) = 2, \text{deg}_{\text{out}}(D) = 1, \text{deg}_{\text{in}}(E) = 1, \text{deg}_{\text{out}}(E) = 1$$

Self-loop: Edge (undirected or directed) is a self-loop if its two endpoints coincide with each other.

Ex:



$$\text{deg}_{\text{in}}(A) = 2$$

$$\text{deg}_{\text{out}}(A) = 3$$